



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS  
General Certificate of Education  
Advanced Subsidiary Level and Advanced Level

**MATHEMATICS**

**9709/41**

Paper 4 Mechanics 1 (M1)

**October/November 2013**

**1 hour 15 minutes**

Additional Materials: Answer Booklet/Paper  
Graph Paper  
List of Formulae (MF9)



**READ THESE INSTRUCTIONS FIRST**

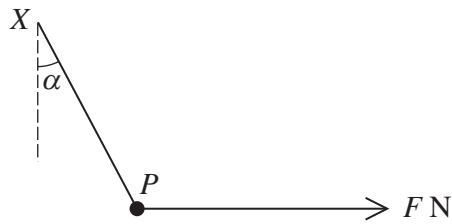
If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.  
Write your Centre number, candidate number and name on all the work you hand in.  
Write in dark blue or black pen.  
You may use a soft pencil for any diagrams or graphs.  
Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.  
Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.  
Where a numerical value for the acceleration due to gravity is needed, use  $10 \text{ m s}^{-2}$ .  
The use of an electronic calculator is expected, where appropriate.  
You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.  
The number of marks is given in brackets [ ] at the end of each question or part question.  
The total number of marks for this paper is 50.  
Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

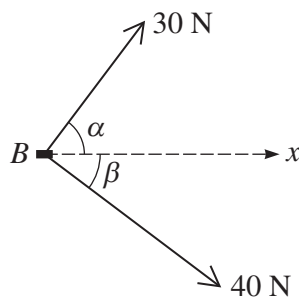
This document consists of 4 printed pages.

1



A particle  $P$  of mass  $0.3 \text{ kg}$  is attached to one end of a light inextensible string. The other end of the string is attached to a fixed point  $X$ . A horizontal force of magnitude  $F \text{ N}$  is applied to the particle, which is in equilibrium when the string is at an angle  $\alpha$  to the vertical, where  $\tan \alpha = \frac{8}{15}$  (see diagram). Find the tension in the string and the value of  $F$ . [4]

2



A block  $B$  lies on a rough horizontal plane. Horizontal forces of magnitudes  $30 \text{ N}$  and  $40 \text{ N}$ , making angles of  $\alpha$  and  $\beta$  respectively with the  $x$ -direction, act on  $B$  as shown in the diagram, and  $B$  is moving in the  $x$ -direction with constant speed. It is given that  $\cos \alpha = 0.6$  and  $\cos \beta = 0.8$ .

(i) Find the total work done by the forces shown in the diagram when  $B$  has moved a distance of  $20 \text{ m}$ . [2]

(ii) Given that the coefficient of friction between the block and the plane is  $\frac{5}{8}$ , find the weight of the block. [3]

3 A cyclist exerts a constant driving force of magnitude  $F \text{ N}$  while moving up a straight hill inclined at an angle  $\alpha$  to the horizontal, where  $\sin \alpha = \frac{36}{325}$ . A constant resistance to motion of  $32 \text{ N}$  acts on the cyclist. The total weight of the cyclist and his bicycle is  $780 \text{ N}$ . The cyclist's acceleration is  $-0.2 \text{ m s}^{-2}$ .

(i) Find the value of  $F$ . [4]

The cyclist's speed is  $7 \text{ m s}^{-1}$  at the bottom of the hill.

(ii) Find how far up the hill the cyclist travels before coming to rest. [2]

- 4 Particles  $P$  and  $Q$  are moving in a straight line on a rough horizontal plane. The frictional forces are the only horizontal forces acting on the particles.

(i) Find the deceleration of each of the particles given that the coefficient of friction between  $P$  and the plane is 0.2, and between  $Q$  and the plane is 0.25. [2]

At a certain instant,  $P$  passes through the point  $A$  and  $Q$  passes through the point  $B$ . The distance  $AB$  is 5 m. The velocities of  $P$  and  $Q$  at  $A$  and  $B$  are  $8 \text{ m s}^{-1}$  and  $3 \text{ m s}^{-1}$ , respectively, both in the direction  $AB$ .

(ii) Find the speeds of  $P$  and  $Q$  immediately before they collide. [5]

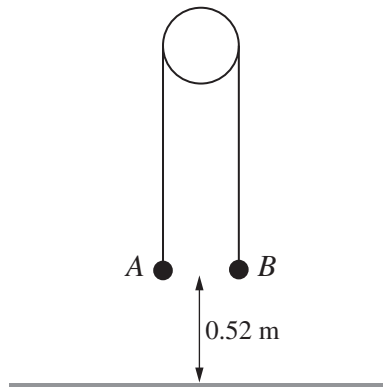
- 5 A lorry of mass 15 000 kg climbs from the bottom to the top of a straight hill, of length 1440 m, at a constant speed of  $15 \text{ m s}^{-1}$ . The top of the hill is 16 m above the level of the bottom of the hill. The resistance to motion is constant and equal to 1800 N.

(i) Find the work done by the driving force. [4]

On reaching the top of the hill the lorry continues on a straight horizontal road and passes through a point  $P$  with speed  $24 \text{ m s}^{-1}$ . The resistance to motion is constant and is now equal to 1600 N. The work done by the lorry's engine from the top of the hill to the point  $P$  is 5030 kJ.

(ii) Find the distance from the top of the hill to the point  $P$ . [3]

6



Particles  $A$  and  $B$ , of masses 0.3 kg and 0.7 kg respectively, are attached to the ends of a light inextensible string. The string passes over a fixed smooth pulley.  $A$  is held at rest and  $B$  hangs freely, with both straight parts of the string vertical and both particles at a height of 0.52 m above the floor (see diagram).  $A$  is released and both particles start to move.

(i) Find the tension in the string. [4]

When both particles are moving with speed  $1.6 \text{ m s}^{-1}$  the string breaks.

(ii) Find the time taken, from the instant that the string breaks, for  $A$  to reach the floor. [5]

[Question 7 is printed on the next page.]

7 A particle  $P$  starts from rest at a point  $O$  and moves in a straight line.  $P$  has acceleration  $0.6t \text{ m s}^{-2}$  at time  $t$  seconds after leaving  $O$ , until  $t = 10$ .

(i) Find the velocity and displacement from  $O$  of  $P$  when  $t = 10$ . [5]

After  $t = 10$ ,  $P$  has acceleration  $-0.4t \text{ m s}^{-2}$  until it comes to rest at a point  $A$ .

(ii) Find the distance  $OA$ . [7]